



EFFECT OF ASPECT RATIO AND INCLINATION ANGLE ON FLUID FLOW AND HEAT TRANSFER IN RECTANGULAR ENCLOSURES

Miraç KAN, Müslüm ARICI and Hasan KARABAY

Kocaeli University, TURKEY

3 - 5 December 2014, Belgrade, SERBIA

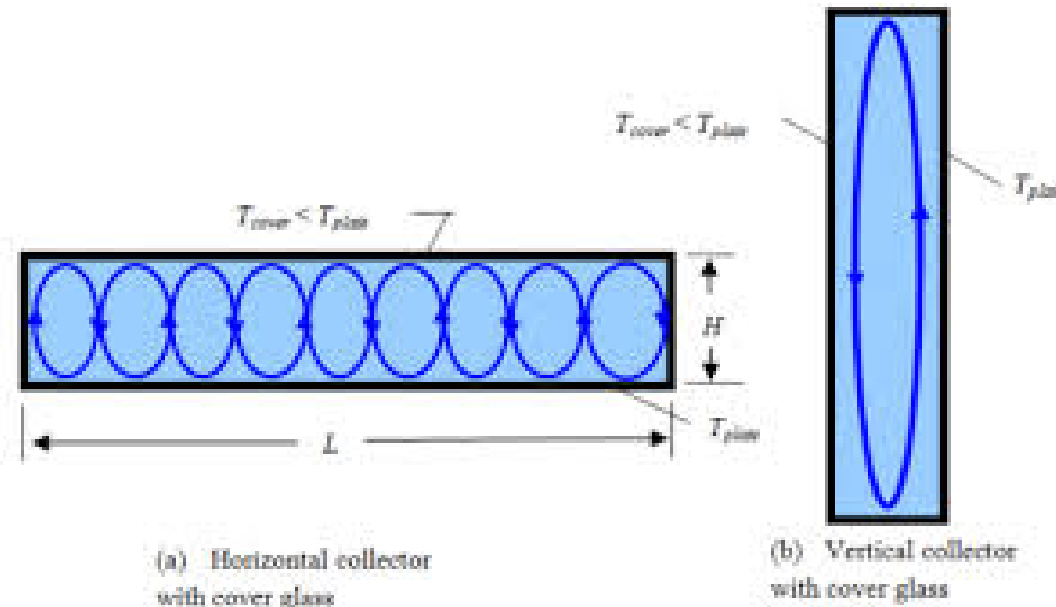
OUTLINE

- ❑ Problem Description
- ❑ Governing Equations
- ❑ Numerical Method
- ❑ Validation
- ❑ Results
- ❑ Conclusion

NATURAL CONVECTION

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Natural convection in rectangular enclosures are encountered in many engineering applications such solar collectors, facades, multiple pane windows, hollow bricks.



PROBLEM DESCRIPTION

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Fluid : Air ($Pr=0.71$)

Flow : Laminar

: Steady

: 2D

: Incompressible

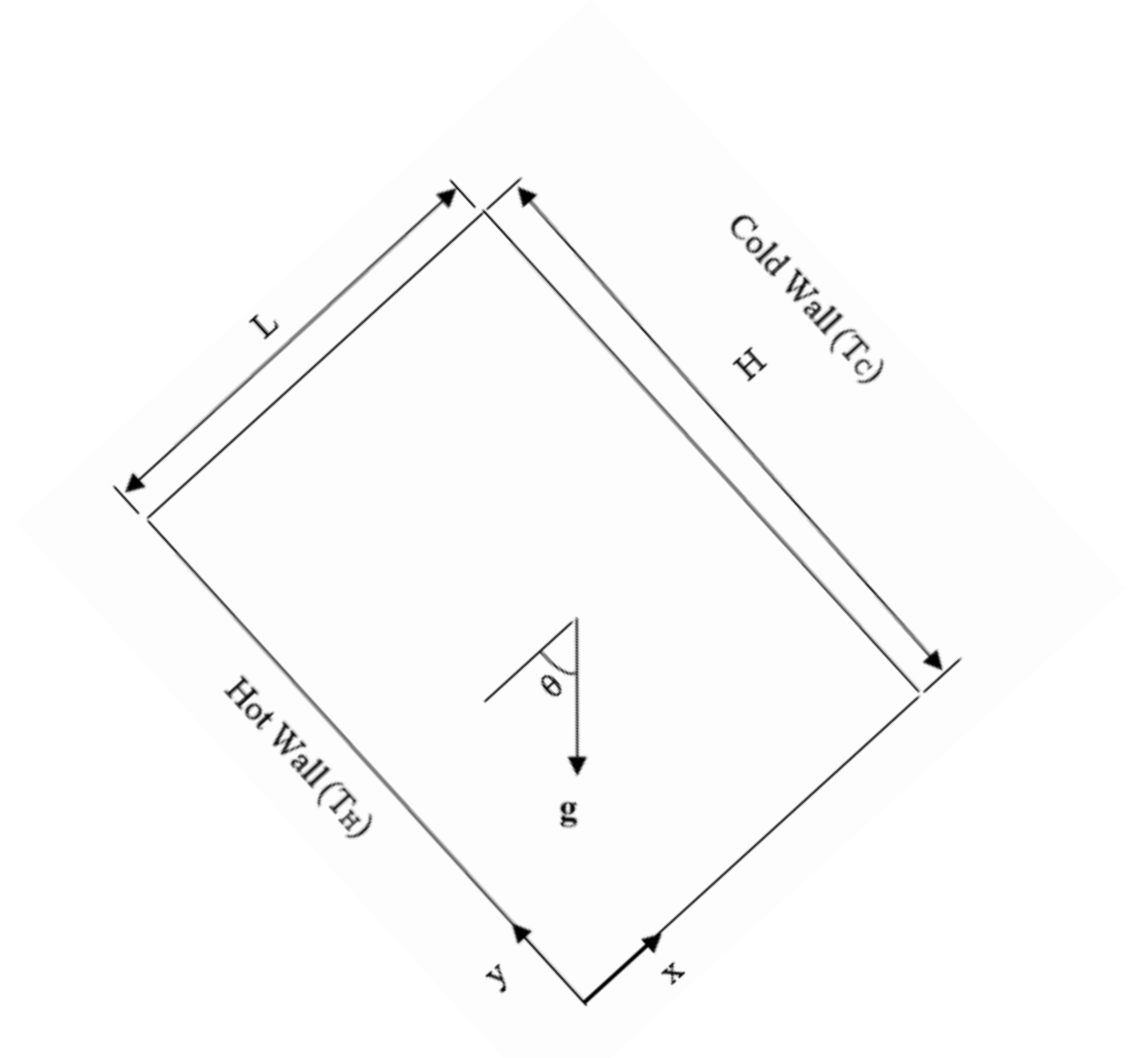
: Boussinesq approximation

$T_C = 293$ K

$T_H = 303$ K

$T_O = 298$ K

Not participating medium

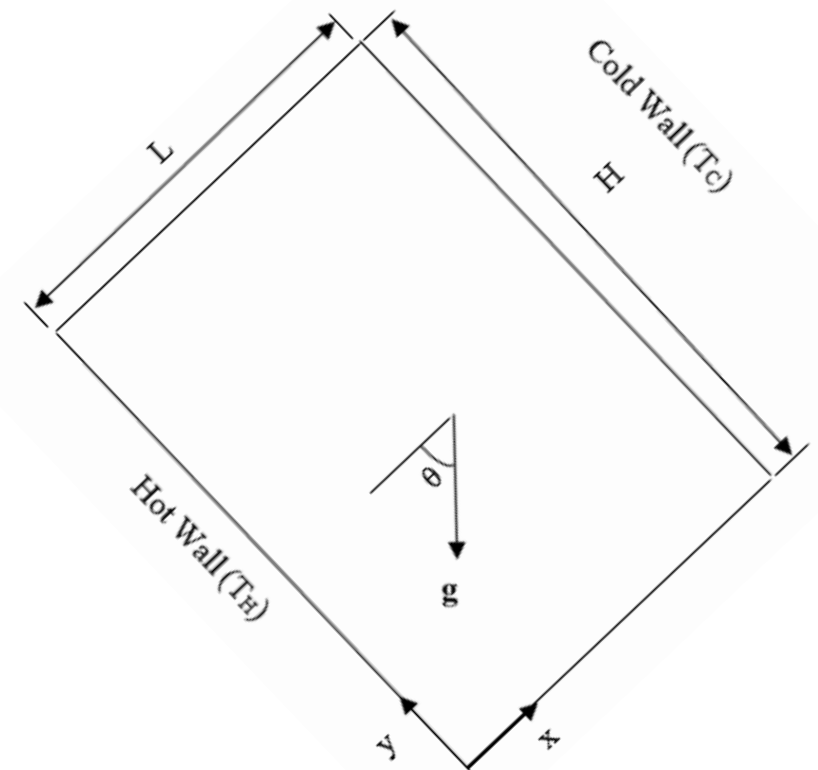


PARAMETERS OF INTEREST

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Rayleigh Number (Ra) $Ra_L = \frac{g\beta\Delta TL^3}{\nu^2} Pr$	$10^3 - 10^4 - 10^5$
Inclination Angle (θ)	$0^\circ - 30^\circ - 60^\circ - 90^\circ - 120^\circ - 150^\circ - 180^\circ$
Aspect Ratio (AR) (H/L)	$1 - 5 - 20$
Emissivity (e)	$0 - 1$
Radiation Number (Nr) $Nr = \frac{\sigma\epsilon T_o^4}{k(T_H - T_C)} L$	$17.40 - 37.48 - 80.75$

Pr=0.71 constant



GOVERNING EQUATIONS

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Continuity:

$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0$$

x-momentum:

$$u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} = -\frac{1}{\rho} \frac{\partial P}{\partial x} + \nu \left(\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} \right) + g\beta(T - T_\infty) \sin \theta$$

y-momentum:

$$u \frac{\partial v}{\partial x} + v \frac{\partial v}{\partial y} = -\frac{1}{\rho} \frac{\partial P}{\partial y} + \nu \left(\frac{\partial^2 v}{\partial x^2} + \frac{\partial^2 v}{\partial y^2} \right) + g\beta(T - T_\infty) \cos \theta$$

Energy:

$$u \frac{\partial T}{\partial x} + v \frac{\partial T}{\partial y} = \alpha \left(\frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2} \right)$$

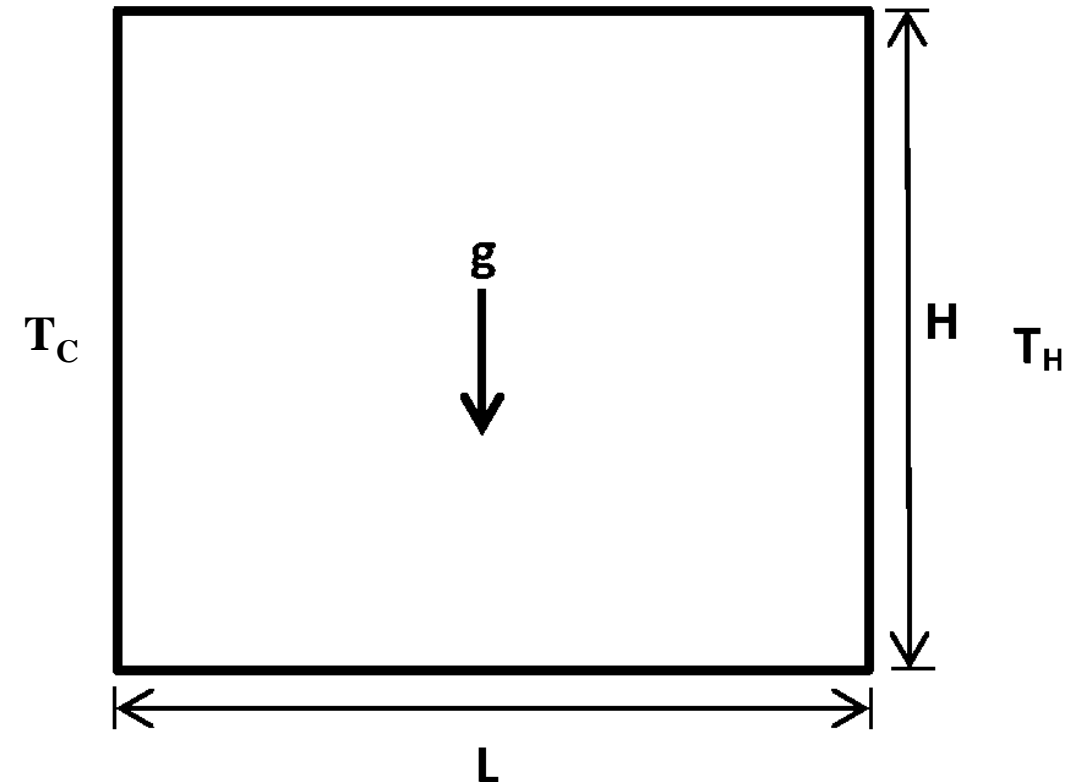
NUMERICAL METHOD

- ❑ Governing equations are solved by ANSYS FLUENT.
- ❑ Second Order Upwind differencing is used to discretize momentum and energy equations
- ❑ SIMPLE algorithm is used to couple Pressure-Velocity.
- ❑ S2S model is used for radiation.
- ❑ Residuals are set to 10^{-5} .

VALIDATION (excluding radiation)

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Rayleigh Number	10^3	10^4	10^5
De Vahl Davis *	1.116	2.234	4.487
Present study	1.115	2.240	4.528
Difference (%)	0.06	0.27	0.91



*G. De Vahl Davis, Natural convection of air in a square cavity a bench mark numerical solution, International Journal for Numerical Methods in Fluids 3 (1983) 249 – 264.

VALIDATION (including radiation)

	$Nu_{\text{convection}}$			$Nu_{\text{radiation}}$		
Rayleigh Number	10^4	10^5	10^6	10^4	10^5	10^6
Akiyama and Chong*	2.1	4.3	8.8	3.2	7.0	15.1
Present study	2.2	4.5	8.9	3.1	6.9	14.9
Difference (%)	4.8	4.7	1.1	2.72	1.67	1.27

*M. Akiyama and Q. P. Chong, Numerical Analysis of Natural Convection with Surface Radiation in a Square Enclosure, Numerical Heat Transfer, Part A: Applications 32 (1997) 419-433.

EFFECT OF INCLINATION ANGLE and ASPECT RATIO ($Ra=10^5$, $\epsilon=0$)

10

AR=1

Streamlines

Isotherms

AR=5

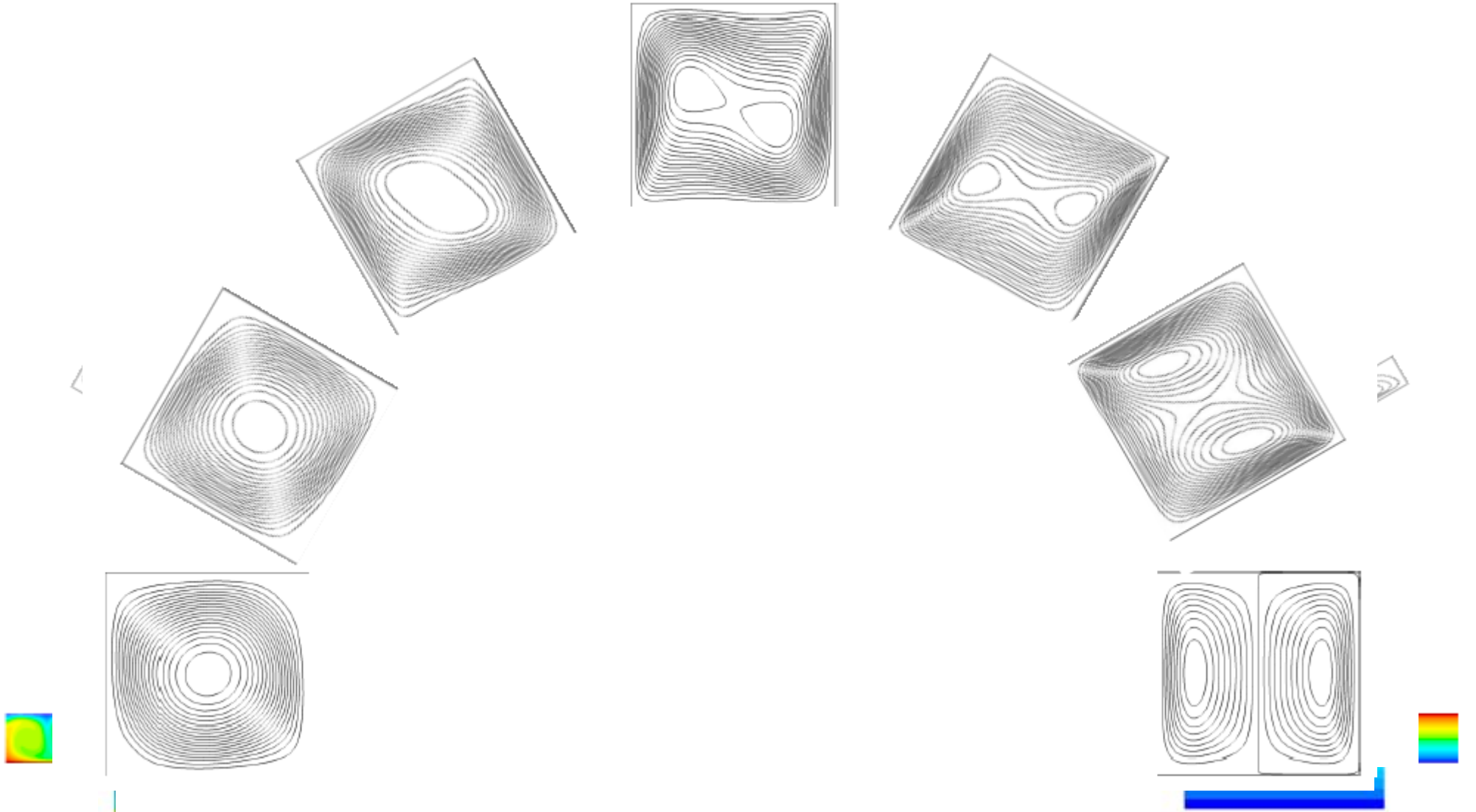
Streamlines

Isotherms

AR=20

Streamlines

Isotherms



EFFECT OF INCLINATION ANGLE and ASPECT RATIO ($Ra=10^5$, $\epsilon=1$)

11

AR=1

Streamlines

Isotherms

AR=5

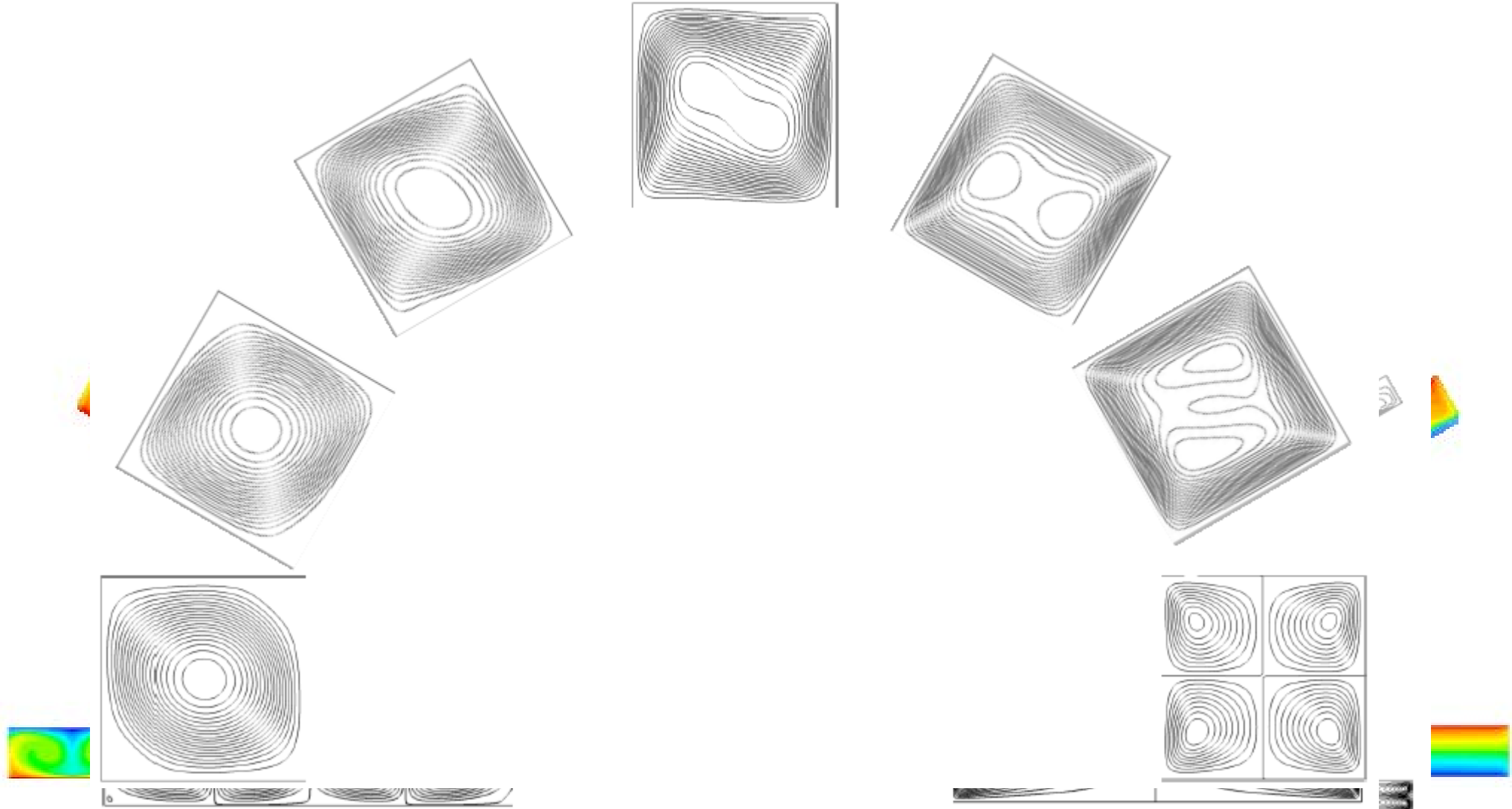
Streamlines

Isotherms

AR=20

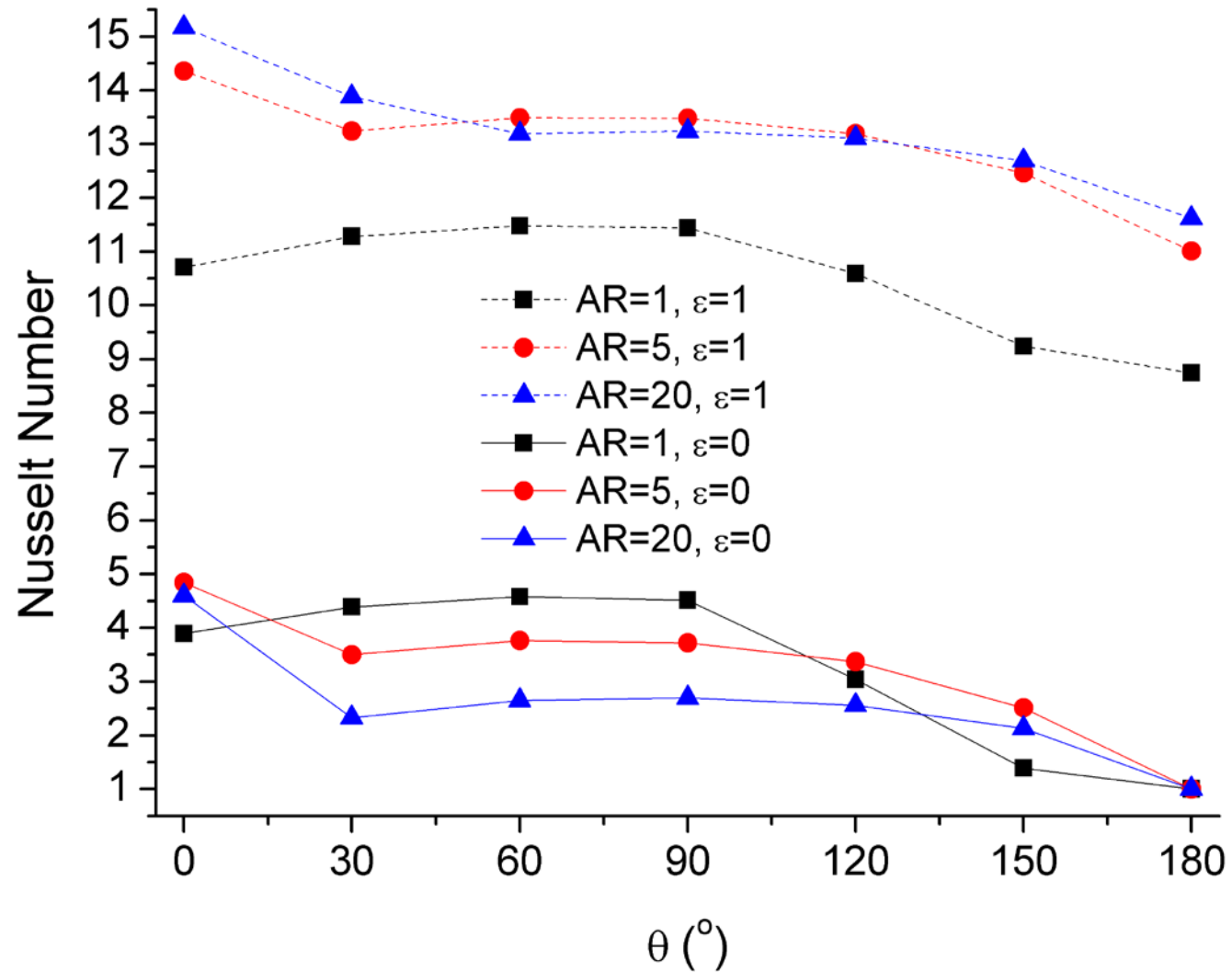
Streamlines

Isotherms



MEAN NUSSELT NUMBER

12

 $Ra=10^3$
 $Ra=10^4$
 $Ra=10^5$


CONCLUSIONS

- When Rayleigh number or aspect ratio increases, Nusselt number increases.
- Aspect ratio has a significant effect on the flow structure particularly for high inclination angles.
- When radiation is not considered, Nu number decreases as AR increases.
- When radiation is considered, Nu number increases as AR is increased from 1 to 5. Nu number decreases slightly as AR is increased from 5 to 20.
- Effect of radiation is more profound in cases where convective heat transfer is not initiated.
- When radiation is taken into account, Nu number increases 2-11 times depending on aspect ratio and inclination angle.

**THANK YOU FOR YOUR
ATTENTION**